

5. BESSEL FUNCTION I, SERIES EXPANSION

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comment Compute the Bessel function $I_n(X)$ when n and X are within the bounds of the series expansion. The procedure calling statement gives n , X and an absolute tolerance δ for determining the point at which the terms of the summation become insignificant. Special case: $I_0(0)=1$;

procedure $I(n, X, \delta) = : (Is)$

begin

I: $s := 0$; $sum := 0$

if $(n \neq 0)$; **go to** STRT

if $(X = 0)$; **begin** $Is := 1$; **return end**

$summ := 1$; **go to** SURE

STRT: $sfac := 1$

if $(s = 0)$; **go to** HRE

for $t := 1$ (1) s

$sfac := sfac \times t$

HRE: $snfac := sfac$

for $t := s + 1$ (1) $s + n$

$snfac := snfac \times t$

$summ := sum + (X/2)^{n+2 \times s} / (sfac \times snfac)$

SURE: **if** $(\delta < \text{abs}(summ - sum))$

begin $s := s + 1$; $sum := summ$; **go to** STRT **end**

$Is := summ$; **return**

end