

## ALGORITHM 17

## TRDIAG

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procedure   trdiag (a,b,c,d) order : (n) result : (x);
value n;    array a, b, c, d, x; integer n;
comment    this procedure gives the solution to the tri-
              diagonal system of linear algebraic equations:
               $a_1x_2 + b_1x_1 + d_1 = 0$ 
               $a_ix_{i+1} + b_ix_i + c_ix_{i-1} + d_i = 0, i = 2,3, \dots, n-1$ 
               $b_nx_n + c_nx_{n-1} + d_n = 0.$ 
              This method is often used to obtain solutions to
              second order difference equations;
begin array gamma [1 : n-1]; integer i; real y;
              gamma [1] := -a[1]/b[1];
              x[1] := -d[1]/b[1];
for         i := 2 step 1 until n-1 do
begin       y = b[i] + c[i] × gamma [i - 1];
              gamma [i] := -a[i]/y; x[i] := -(c[i] × x[i-1]
              + d[i])/y end;
              x[n] := -(c[n] × x[n-1] + d[n])/(b[n] + c[n]
              × gamma [n-1]);
for         i := n step -1 until 2 do
              x[i - 1] := x[i] × gamma [i - 1] + x[i - 1]
end trdiag

```